

June 12, 2025 | Fusion Energy Division
Integrated Plasma Modeling:

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From the Power of the Sun to Powering Society on Earth

#### PRESENTED BY

### Sebastian De Pascuale

PPPL SULI Introduction to Fusion Energy and Plasma Physics Summer School Course



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### **About Me – From Astronomy to Space Physics**



#### **Grinnell College**

**University of Iowa** 



### About Me – From Water Rocketry to Rowing on Water



Knox County, Ohio

Knox County, Tennessee



### My Trajectory into the Field of Fusion Energy Science







2011 – Los Angeles Research Experiences for Undergraduates (REU) 2015 - Los Alamos Space Weather Summer School (SWSS) 2018 - Oak Ridge Post-Doctoral Research Associate (ORNL)



"Just as the system of the sun, planets and comets is put in motion by the forces of gravity, and its parts persist in their motions, so the smaller systems of bodies also seem to be set in motion by other forces and their particles to be variously moved in relation to each other and, especially, by the electric force"

Sir Isaac Newton, Principia (1687)



# **Exploring Dusty Horizons at University of California, Los Angeles**



"Your reward will be the widening of the horizon as you climb" - Cecilia Payne (figure from NASA's Mars Perseverance Rover)

#### \*Undergraduate Mentor Dr. Michael Fitzgerald

### CAK RIDGE

https://www.eso.org/public/images/eso0842b/

https://science.nasa.gov/wp-content/uploads/2023/04/fomalhaut\_labeled-jpg.webp

### How do you find exoplanets orbiting other stars?

• Observe light curves from the occlusion of a planetary body in front of a star, or observe the gravitational disturbance of smaller bodies to the surrounding circumstellar debris disk





• Dust grain sized particles scatter light preferentially in the forward direction under Mie theory, causing the zodiacal light observed on Earth or the reddish haze observed on Mars



#### https://usfusionenergy.org/opportunities



Illustration by Thumỹ Phan for U.S. Fusion Outreach

### Cecilia Payne

What are stars made of? How do stars make their energy? We know the answers to these questions thanks to Dr. Cecilia Payne-Gaposchkin, who discovered that the stars, like our Sun, are mostly made of hydrogen and helium. This led to our understanding of fusion—the reaction that powers our sun and the stars. These elements are the "fuel" that powers fusion reactions inside the sun in a giant fusion engine. Together, we are working to build fusion engines here on Earth. Join the celebration and join the movement to bring the power of the stars to Earth.



# **Pursuing Complex Science at Los Alamos National Laboratory**

#### How does space weather impact life on Earth?

 Geomagnetic storms are caused by the plasma connection of Earth's magnetosphere with the enveloping solar heliosphere drawn out by coronal mass ejections and solar wind and flares





• Radiation belts trap energetic charged particles and can pose operational risks to commercial, national, and scientific satellites



"I think the next [21<sup>st</sup>] century will be the century of complexity" -Stephen Hawking (figure from NASA GSFC Fleet ID:14718)

- \*Thesis Advisor Dr. Craig Kletzing and Vania Jordanova
- □ De Pascuale et al., JGR Space Phys., 2018 https://doi.org/10.1029/2018JA025776

### 14<sup>TH</sup> ITER INTERNATIONAL SCHOOL

30 June (Monday) – 4 July (Friday) 2025 Aix-Marseille University, Aix-en-Provence, France

### INTEGRATED MODELLING IN MAGNETIC FUSION PLASMAS

The subject of the 2025 school is 'Integrated Modelling in Magnetic Fusion Plasmas.' Reliable predictions of (TER plasmas—spanning the entire cross-section from the plasma core and scrape-off layer (SOL) to the material surface—are critical for achieving (TERs fusion power demonstration goals. Such predictions are indispensable for defining and preparing plasma operational scenarios, analyzing the plasma pulses planned for (TER, and evaluating required control schemes via simulations of measurements, actuators, and plasma responses.



### **Summer Schools**

ITER International School is organized nearly every year to offer early career scientists and engineers multi-disciplinary networking and instruction on the exciting field of nuclear fusion.

Each school is organized around a specific scientific theme and hosted by different countries around the world at institutions with access to tours of experimental research facilities.

Previous topics include:

- Diagnostics and Data Science
- Impacts of Energetic Particles
- Operation Scenarios and Control
- Technology of Power Flux Handling
- Transport and Pedestal Physics
- Disruptions and Magnetohydrodynamics
- High Performance Computing
- Plasma-Surface Interactions





# Solving Big Problems at Oak Ridge National Laboratory



"We need people [at Oak Ridge] to solve big problems" - Eugene Wigner (figure from ORNL Main Campus)

#### \*Post-doc Advisor Dr. David Green

De Pascuale et al., J. Comp. Phys., 2023 https://doi.org/10.1016/j.jcp.2023.112089

#### How can we accelerate progress towards fusion?

• High fidelity fusion simulations are computationally prohibitive without accounting for numerical limitations on the treatment of multiple scales







 Sparse discretization methods in space and time offer tractable approaches to reduce computational overhead and develop reduced models of governing physical systems



### **Research Internships**

ORNL educational programs provide experiences complementing academic programs and enabling opportunities for additional learning, development, and training in a laboratory workplace setting.

Commitment to enriching scientific culture and the future workforce through **learning objectives** based, **mission aligned** experiences with world-class researchers, staff, facilities.

Over **20 program offerings** are available at any point in your developing career including elementary education, high school, undergraduate, community college, and graduate student participants.

See you at the traveling science fair or during a fall, spring, or summer internship!



https://education.ornl.gov





### **Three Takeway Themes**

#### QUANTUM

Empowering scientists to pursue quantum innovation



#### FUSION

Fusion energy project among six ORNL Federal Laboratory Consortium wins



ΑI

Leading research to ensure secure, trustworthy, and energy efficient AI







Pearce et al., Proc. Natl. Acad. Sci, 2014; https://doi.org/10.1073pnas.1402202111

Cavagna et al., Nat. Comm., 2022; https://doi.org/10.1038/s41467-022-29883-4

### **First in Flight**

"The period from 1885 to 1900 was one of unexampled activity in aeronautics, and for a time there was high hope that the age of flying was at hand...

But the public, discouraged by the failures and tragedies it had just witnessed, considered flight beyond the reach of humans, and classed its adherents with the inventors of perpetual motion...

Heavier-than-air flight had been around the corner for decades, with little to show for it..."



# Flying, with Contemporary Style



Fly-by-the-seat-of-your-pants

Fly-by-wire







### Flying, with Common Sense







### From Flight Simulator to Pulse Simulator







### **Designing a Digital Twin**





### First in Fusion – Putting Another Star on the Map

"Fusion is unquestionably one of the key technologies that will shape the coming millennium" following energy crisis of the 70s

In the 1980's Governor Alexander had a vision to create an Oak Ridge Corridor, and by 1995 an annual Science & Technology Summit was convened

During this time, fusion scaled back in enthusiasm, but reached new world records as well as substantial technological challenges

In 2010 "**Thirty years later**, tomorrow is here and –despite some delay– so is the bright promise" on ITER



# Tennessee's nuclear renaissance

East Tennessee's nuclear industry is growing rapidly. Businesses are introducing new reactor and fuel designs. Institutions such as ORNL, the Tennessee Valley Authority and the University of Tennessee are providing knowledge and support. And local colleges are ensuring this growing industry has a skilled workforce. Here are just a few of the region's major players.



#### **FUTURE FUSION ENERGY HUB**

https://www.ornl.gov/nuclearishere



### Building Bridges for Public-Private Partnerships to Enable a Thriving Fusion Workforce and Industry Ecosystem



https://www.energy.gov/fusion-energy



https://typeoneenergy.com/potential-site-for-stellarator-fusion-prototype-machine-identified/

# Transport Processes are Inherently Multi-Scale and Ubiquitous Across the Entire Fusion Plasma System



#### **Core Confinement**

• Maintain plasma performance under turbulence and other loss mechanisms

#### **Edge Stability**

• Manage high density and temperature against magnetohydrodynamic effects

### **Power & Particle Exhaust**

• Mitigate plasma facing component exposures to damaging conditions

A hierarchy of simulation fidelities are required to achieve self-consistent tokamak plasma solutions

aboratory \*Adapted from Giacomin et al., (2022), JCP, 463, 111294

### **Physics of Gyrokinetic Turbulent Transport in Tokamaks**





# Impact of Steep Gradients on Tokamak Edge Pedestal



#### **Characteristic DIII-D Pedestal Scales**

**CAK RIDGE \*Bonoli et al., 2015** 

### **Consequence of Tokamak Power Exhaust and Particle Control**







**CAK RIDGE** [Arnas, et al., *Nuc. Mat. Energy* 2017 (Alcator C-Mod)

# **Integrated Modeling Captures Key Physics Regimes to Constrain Conditions on Behavior of Plasma Dynamics**





### **Components of Experimental Control and Reactor Design**

Tokamak Operations

**Tokamak Simulations** 





### **Components of Experimental Control and Reactor Design**

#### **Massively Parallel File-Based Model Coupling**





### **Components of Experimental Control and Reactor Design**



#### Tokamak Shot Cycle

#### **Integrated Plasma Simulator**





### Reduced Models of Turbulent Transport Bridge Nonlinear Scales through Projected Linear Physics to Converged Saturation Level



National Laboratory \*GENE simulation and Dudding et al., Nucl. Fusion, 2022; https://doi.org/10.1088/1741-4326/ac7a4d

### **Saturation Rules Employ Multi-Fidelity Modeling to Capture Complex Interaction Between Physical Plasma Parameters**

 $\left< \left| \delta \hat{\theta}_{kx,\,k_y} \right|^2 \right>_{ heta,\,t/} \phi_{\mathrm{uni}}^2$ 

50

40

30

20 10 0

1.0 0.5

0.0 -0.5 + 9001t

-1.0



#### Saturated Potential

#### **Physical Parameter Space**

Nucl. Fusion 62 (2022) 096005

H.G. Dudding et al

Table 1. Details of the 43 nonlinear CGYRO simulations that form the database. Note that the labels in the second column correspond with those in figure 13(c), used for discerning the cases displayed in figures 13(a) and (b), 17 and 18.

Varied parameter	Values (label)	Fixed	Isotopes simulated
- (GA-std)	— (a)	_	H, D, T
$a/L_{T_i} = a/L_{T_e}$	1.5 (b), 2.25 (c), 3.5 (d)	_	H, D, T
$a/L_n$	2.0 (e), 3.0 (f)	_	H, D, T
ŝ	0.25 (g), 0.5 (h), 1.5 (i)	$\hat{s}/w = 1/4$	D
$(a/c_s)\nu_{ee}$	0.01 (j)		H, D, T
$(a/c_s)\nu_{ee}$	1.0 (k)	_	D
$T_{\rm i}/T_{\rm e}$	0.5 (l), 1.5 (m)	_	D
q	1.5 (n), 2.5 (o)	_	D
κ	1.25 (p), 1.5 (q), 2.0 (r)	_	D
Δ	-0.125 (s), $-0.25$ (t), $-0.5$ (u)	_	D
$r_0/R_0$	1/4 (v), 1/12 (w)	_	D
$(a/c_s)\nu_{ee}$	0.01 (x)	$a/L_n = 3.0$	H, D, T
$(a/c_s)\nu_{ee}$	0.05 (y)	$a/L_n = 3.0$	H, T
$(a/c_s)\nu_{\rm ee}$	1.0 (z)	$a/L_n = 3.0$	D

$$k_y, \gamma, \omega \rightarrow \phi^2$$

### Global Quasilinear Transport is Governed by High-Dimensional Parameter Space Prohibiting Comprehensive Model Sampling



Express curse of dimensionality when increasing degrees of freedom

QuaLiKiz 15D, Ho et al., (2020), PoP, 28, 032305

Dataset	Points	Time (CPU h)	
10D	$\sim 3 \times 10^8$	$\sim \! 10^{6}$	
Projected 15D	$\gtrsim$ 7.2 $ imes$ 10 <sup>10</sup>	$\gtrsim 3  imes 10^8$	
Actual 15D	$3.38  imes 10^7$	$3.5  imes 10^5$	

Supplement training data through experimental observations



https://zenodo.org/records/3274234

**TGLF 21D**, Menenghini et al., (2014), *PoP*, 21, 060702 **TGLF 23D**, Menenghini et al., (2017), *NF*, 57, 086034

https://zenodo.org/records/3274234

**QuaLiKiz 4D**, Citrin et al., (2015), *NF*, 55, 092001 **QuaLiKiz 6D**, Citrin et al., (2023), *PoP*, 30, 062501 **QuaLiKiz 10D**, van de Plassche (2020), *PoP*, 27, 022310

Fully 5D gyrokinetic simulations take on the order of 10<sup>4</sup> hours of wall clock time per radial point



### Local Dimensionless Plasma Parameters Have Associated **Correlations and Accessibility in Present and Future Device**



Gyrokinetic validation data is several orders of magnitude more expensive

TGLF-GKNN, Neiser et al., (2024) TTF Conference

Saturation Rule	Validation	Machines
SAT0,1,2,3	CGYRO	DIII-D/MAST-U

Supplement quasilinear model performance through residual





#### Quasilinear models, such as the **Trapped Gyro Landau Fluid (TGLF)**, reduce this cost down to **10<sup>o</sup> seconds**



### Matrix Factorization Cannot Fully Capture Nonlinear Relationships in Feature Space of Simulation Domain

Variable	Definition
rla	Normalized minor radius
R/a	Normalized major radius
$\kappa$	Elongation
$r\frac{\partial\kappa}{\partial r}$	Elongation shear
$\delta^{r}$	Triangularity
$\frac{\partial R}{\partial R}$	Shafranov shift
дr a	Safety factor
$\frac{q^2a^2}{2}\frac{\partial q}{\partial q}$	Safety factor shear
$\beta_{e}^{r^{2}} \partial r$	Kinetic to magnetic pressure ratio
$\nu_{\rm ie}/ac_s$	Collision frequency
$T_{\rm i}/T_{\rm e}$	Ion to electron temperature ratio
$n_{\rm D}/n_{\rm e}$	Deuterium to electron density ratio
$n_{\rm C}/n_{\rm e}$	Carbon to electron density ratio
$Z_{\rm eff}$	Effective ion charge
$a/L_{\mathrm{Te}}$	Electron temperature scale length
$a/L_{ m Ti}$	Ion temperature scale length
$a/L_{ne}$	Electron density scale length
$a/L_{n\mathrm{D}}$	Deuterium density scale length
$a/L_{nC}$	Carbon density scale length
$\frac{qa^2}{rB^2}\frac{\partial p}{\partial r}$	Total pressure gradient
$\operatorname{sign}(I_{\mathrm{p}})R\omega_{\mathrm{tor}}\frac{a}{c_{\mathrm{s}}}$	Parallel velocity
$-\mathrm{sign}(I_{\mathrm{p}})R\frac{\partial\omega_{\mathrm{tor}}}{\partial r}\frac{a}{c_{\mathrm{s}}}$	Parallel velocity gradient
$-\mathrm{sign}(I_{\mathrm{p}})\frac{r}{q}\frac{\partial^{\frac{V_{E\times B}}{R}}}{\partial r}\frac{a}{c_{\mathrm{s}}}$	$E \times B$ velocity shear

Menenghini et al., (2017) NF, 57, 086034

CAK RIDGE



Surveyed database of DIII-D TGLF simulations spans **24D inputs** and **6D outputs** over range of experimental conditions and nearly 1.6 million points

### Vector Quantization Groups Nearest Neighbor Simulations Separating Out Over-Sampled Parameter Regions in Domain



Dataset can be compressed by nearly an **order of magnitude** when clustered in the input space alone, reducing the number of simulations required for machine learning



### Accelerated Predictions of Quasilinear Transport Simulations in Many Degrees of Freedom Are Enabled by Machine Learning



\*12 branch max depth, 80/20 percent train-test-split

### Sensitivity of Surrogate Modeling Framework is Captured by Computationally Tractable Calculation Over Large Datasets

**Shapley values**: game theoretic description of importance distribution over possible features

- 1. additive explanation of each parameter for each prediction
- 2. interaction of each parameter to overall model behavior
- 3. dominant feature selection for each independent output



**Neural Network** 





target

#### Ion Momentum Flux



### Target Predictions are Evaluated in Terms of Parameter Marginal Contributions Across All Possible Coalitions



#### **Outlier Model Prediction**

Predictions exhibit contrasting characteristic response to model input parameters



Matched Model Prediction

### Transport Simulations Can be Augmented with Expanded Search Around Particular Coordinate Set Combinations

#### **3 Neighbors Identified as Outliers**

#### 52 Neighbors within 10% of Target



Simulations sparsely cover proximal experimental conditions near extrema



### Survey of Database Indicates Parameter Interaction Strengths In Terms of Degree and Direction of Model Importance

Ion Momentum Flux



Ion Energy Flux

### Model sensitivity reveals significant partial populations providing minimal impact



### **Explainable Machine Learning Unlocks Physical Insight to Determine Parameter Interdependence for Efficient Sampling**



**Paired Model Contributions** 

\*See M. Landreman et al., 2025 arXiv:2502.11657 for extensive application to stellarator transport simulations 41

### **Explainable Machine Learning Unlocks Physical Insight to Determine Parameter Interdependence for Efficient Sampling**

**Total Parameter Contributions** 



**Shapley Value Assessment** 



\*See M. Landreman et al., 2025 arXiv:2502.11657 for extensive application to stellarator transport simulations 42

### Drastic Reduction in Degrees of Freedom by Feature Importance Sampling of Surrogate Model Shapley Values

24 Input Components

4 Input Components Selected by Shapley





### Similar Studies Provide Data-Driven Insight from Machine Learning on Stellarator Turbulent Transport Configurations

#### **Shapley Value Parameter Contribution**



#### **Quasi-Axisymmetric Configurations**



**CAK RIDGE** National Laboratory Landreman et al., (2025), arXiv: 2502.11657, \*ITG only

### **Taking Interpretable Machine Learning One Step Further**



### **Operational Performance Can be Governed by Key Observable Quantities Linking Actuators to Divertor Targets**



Stangeby, Plasma Phys. and Control. Fusion 2018]

ational Laboratory

### Dynamics are Best Characterized by Inverse Dependence of Key Plasma State Variables on Outer Divertor Target









- Data rescaling allows for physically consistent exploration of input parameter space for determination of controlled trajectories
- Identified coupled nonlinear equations are not sparse, but can be analyzed for stability characteristics to prevent over-fitting

Lore et al., Nucl. Fusion, 2023 https://doi.org/10.1088/1741-4326/acbe0e

### Integration of Workflow Demonstrates Unique Capability for **Evaluation of Strategies for Performance Optimization**

**Process Variables** 

 $+ m_{2} - 1$ 

 $i + m_{-}$ 

2.8

0.00

0.01

**Target Setpoint** 



#### Model predictive control minimize cost function subject to constraints on input and output quantities

**IPS-FASTRAN** provides framework for SOLPS-ITER runs with feedback from extracted reduced models

$$J = \left\| x_{j+m_p} - \tilde{x}_{m_p} \right\|^2 + \sum_{k=0}^{m_p - 1} \left\| x_{j+k} - \tilde{x}_k \right\|^2 + \sum_{k=1}^{m_c - 1} \left\| u_{j+k} \right\|^2 + \left\| \Delta u_{j+k} \right\|^2$$

JAK KIDGE [Kaiser, et al., Proc. Royal Soc. A. 2018]; [Lore, et al., Nucl. Fusion, 2023] National Laboratory

#### **IPS-FASTRAN** Implementation 1e19 3.225 3.200 Ε 3.175 target setpoint @OMP, 3.150 3.125 3.100 prediction horizon ⊆ 3.075 0.00 0.01 0.02 0.03 0.04 0.05 5.6 e< 5.4 T<sub>e,sep</sub>@O.Div, 5.2 5.0 4.8 4.6 0.00 0.01 0.02 0.04 0.05 0.03 1e21 3.8 s, 3.6 -3.4 -3.2 control interval даs 0.С даs $m_p$ $m_c$

0.02

time. s

0.03

0.04

0.05

#### Science Highlight from SULI Program Internship – A. Irvin (UTK) **CAK RIDGE** National Laboratory

#### **Scientific Achievement**

- Surrogate model accelerates FPP design and optimization of plasma profile control system utilizing electron cyclotron heating and current drive
- 25x reduction in compute time to generate electron cyclotron heating and current drive profile predictions based on 9 free parameters



#### **Significance and Impact**

- Surrogate model of TORAY ray tracing code provides rapid predictions with uncertainty quantification
- Inverse-solvable model can predict inputs needed to generate a desired output without the need for large parameter scans for rapid optimization

EC

EC

Current

Density

0.2

Heating

0.05

(zE 0.04

¥ 0.03

Q.02

0.01

0.020

0.015

£ 0.010

0.005

0.000

0.0

#### □ Irvin et al., Fus. Sci. and Tech., 2025 https://doi.org/10.1080/15361055.2025.2476829

#### **Research Details**

- Former SULI/ECO internship (E. Hassan and S. De Pascuale) and current UT-Knoxville graduate student assistantship (L. Casali)
- Regression using database of 1600 points for a compact advanced tokamak (CAT) using IPS-TokDesigner



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### **Three Takeway Themes**





### The Integrated Plasma Simulator (IPS) Framework is Enabling Surrogate Model Development for Online Coupled Workflows

- Accelerate expensive simulation of core transport and pedestal stability within a coupled framework
- Predict plasma boundary response to core and pedestal conditions during detachment control
- **Quantify** uncertainty in machine learning surrogate models for decision-ready tokamak pulse simulation

These aims enable fast tokamak pulse simulation for:

- 1. <u>Reactor design</u> leveraging physics informed and Bayesian inference neural networks to reduce dimensionality of coupled simulations
- 2. <u>Session planning</u> leveraging data assimilation and adaptive sampling to constrain predictions of operational space



#### Multi-Fidelity Model Coupling Framework

### **Code-Piloting Advanced Simulations for Reactor Digital Twins**



Advanced Profile Prediction for Fusion Pilot Plant Design PI: D. Ernst at MIT (FIRE 2024 to 2028) **Trustworthy Multiscale Probabilistic Turbulence Foundation Models** PI: P. Zhang at ORNL (LDRD 2023 to 2026)

**CAK RIDGE** National Laboratory [Federici, et al., *NF*. 2021; https://arxiv.org/abs/2412.20601]  $\Gamma_{\perp} \propto D_{\perp}, \chi_{\perp} \left(\frac{\partial}{\partial r}\right) n, T$ 

### **About You – Where will your science story go from here?**

"Remember to look up at the stars and not down at your feet. Try to make sense of what you see and wonder about what makes the universe exist. Be curious" – Stephen Hawking



#### **ITER Tokamak**

**W7-X Stellarator** 



"In science, it is not speed that is most important. It is the dedication, the commitment, the interest and the will to know something and understand it" – Eugene Wigner





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### Multi-Parameter Mapping of Input Space to Targeted Output Quantities for Reduced Simulation Scans of TGLF Sensitivity

Variable	Definition			
rla	Normalized minor radius			
R/a	Normalized major radius			
$\kappa$	Elongation			
$r\frac{\partial\kappa}{\partial r}$	Elongation shear			
$\delta r$	Triangularity			
$\partial R$	Shafranov shift			
∂r <b>q</b>	Safety factor	Energy Flux 1 (6)	Energy Flux 2 (7)	Momentum Flux 2 (7+)
$q^2a^2 \partial q$	Safety factor shear			
$\frac{r^2}{\beta_r} \frac{\partial r}{\partial r}$	Kinetic to magnetic pressure ratio			
$\gamma_{e}$	Collision frequency	• VFA		<ul> <li>VEXB+SHEAR</li> </ul>
$T_{\rm i}/T_{\rm e}$	Ion to electron temperature ratio	• BFT.	AF	
$n_{\rm D}/n_{\rm e}$	Deuterium to electron density ratio	DEN		<ul> <li>KAPPA_LOC</li> </ul>
$n_{\rm C}/n_{\rm e}$	Carbon to electron density ratio	• RLN	S_1/2	
$Z_{\rm eff}$	Effective ion charge		C 1/2	<pre> • F_FKIIVIE_LCO </pre>
$a/L_{\mathrm{Te}}$	Electron temperature scale length	• KLI	5_1/2	
$a/L_{ m Ti}$	Ion temperature scale length			
$a/L_{ne}$	Electron density scale length	Particle Flux 1 (6)	Particle Flux 2 (7)	Particle Flux 3 (6)
$a/L_{n\mathrm{D}}$	Deuterium density scale length			
$a/L_{nC}$	Carbon density scale length			
$\frac{qa^2}{r^2}\frac{\partial p}{\partial r}$	Total pressure gradient			
$rB_{\text{unit}}^2 \partial r$	Parallel velocity			
$sign(I_p)K\omega_{tor} - \frac{1}{c_s}$	Taraner velocity		<ul> <li>DRMAJDX_LUC</li> </ul>	
$-\operatorname{sign}(I_n)R^{\frac{\partial\omega_{\operatorname{tor}}}{a}}$	Parallel velocity gradient		VPAR SHEAR 1	
$\partial r c_{\rm s}$			VI AN_OILAN_I	
$\partial \frac{V_{E \times B}}{R}$	$E \times B$ velocity shear		• RLNS_1/2/3	
$-\operatorname{sign}(I_p)\frac{r}{q}\frac{r}{\partial r}\frac{u}{c_s}$				
			• AS_Z/3	
24 In	put Dimensions			

### **Particular Challenge in Capturing Momentum Flux Variability**





	TG	LF-NN-23D	
Variable	Definition	Database	Output
r/a	Normalized minor	RMIN_LOC	OUT_tur_ENERGY_FLUX_1
	radius		
R/a	Normalized major	RMAJ_LOC	OUT tur ENERGY FLUX i
	radius		
κ	Elongation	KAPPA_LOC	OUT_tur_PARTICLE_FLUX_1
<i></i> ∂κ	Elongation shear	S_KAPPA_LOC	OUT tur STRESS TOR i
$r \frac{1}{\partial r}$			
δ	Triangularity	DELTA_LOC	OUT_tur_PARTICLE_FLUX_2
$\partial R$	Shafranov shift	DRMAJDX_LOC	OUT_tur_PARTICLE_FLUX_3
$\overline{\partial r}$			
q	Safety factor	Q_LOC	
$q^2 a^2 \partial q$	Safety factor shear	Q_PRIME_LOC	
$r^2 \overline{\partial r}$			
$\beta_e$	Kinetic to magnetic	BETAE	
	pressure ratio		
$v_{ie}/ac_s$	Collision frequency	XNUE	
$T_i/T_e$	Ion to electron	TAUS_2	
	temperature ratio		
$n_D/n_e$	Deuterium to electron	AS2	
	density ratio		
$n_c/n_e$	Carbon to electron	AS3	
	density ratio		

Z <sub>eff</sub>	Effective ion charge	ZEFF
$a/L_{Te}$	Electron temperature scale length	RLTS_1
$a/L_{Ti}$	Ion temperature scale length	RLTS_2
$a/L_{ne}$	Electron density scale length	RLNS_1
$a/L_{nD}$	Deuterium density scale length	RLNS_2
a/L <sub>nC</sub>	Carbon density scale length	RLNS_3
$\frac{qa^2}{rB_{unit}^2}\frac{\partial p}{\partial r}$	Total pressure gradient	P_PRIME_LOC
$sign(I_p)R\omega_{tor}\frac{a}{c_s}$	Parallel velocity	VPAR_1
$-sign(I_p)R\frac{\partial\omega_{tor}}{\partial r}\frac{a}{c_s}$	Parallel velocity gradient	VPAR_SHEAR_1
$-sign(I_p)\frac{r}{q}\frac{\partial \frac{V_E \times B}{R}}{\partial r}\frac{a}{c_s}$	E x B velocity shear	VEXB_SHEAR
$\lambda_D$	Debye length/gyroradius	DEBEYE

