### Dynamos and Reconnection in Laboratory and Astrophysical Plasmas

#### Fatima Ebrahimi

Princeton Plasma Physics Laboratory and Dept. of Astrophysical Sciences, Princeton University

#### 2017 PPPL Summer SULI Thursday Seminar July 13, 2017





### Magnetic fields are observed to exist essentially everywhere in the universe



#### Galactic, geo, solar magnetic field

#### (Loading sunexplosion.mp4)



#### Why is the universe magnetized?



Examples of self-organized plasmas include **Flow-dominated**: astrophysical disks **Magnetically-dominated**: surface of stars (disk and stars coronas).



#### What do we know about magnetic fields?

 Energy and flux are the most familiar global quantities of magnetic fields. How about the topological property?

Magnetic helicity, a topological property, measures the knottedness and the twistedness of magnetic fields



$$Bd\mathbf{v}_1 = B \cdot \hat{n}ds_1dl_1 = \Phi_1dl_1$$

$$\begin{aligned} & K_1 = \int \mathbf{A} \cdot \mathbf{B} d\mathbf{v}_1 \\ &= \Phi_1 \int \mathbf{A} \cdot dl_1 = \Phi_1 \Phi_2 \end{aligned}$$

Two interlinked flux tubes  $\longrightarrow$ 

It can be shown that magnetic helicity is a rugged invariant

$$K = \int A \cdot B dV = 2 \phi \phi$$



### Dynamo converts fluid kinetic energy into magnetic energy:

$$ho V^2 \Rightarrow B^2/2\mu_0$$

- "Large-scale dynamo"- the generation of large-scale field accompanied by the generation of total magnetic flux.
- "Small-scale dynamo" sustainment of magnetic energy due to magnetic fluctuations in a turbulent state with a small amount of flux.

Signatures of dynamo: production of magnetic energy, flux and helicity out of no, or seed, field



### Dynamo converts fluid kinetic energy into magnetic energy:

$$\rho V^2 \Rightarrow B^2/2\mu_0$$

- "Large-scale dynamo" the generation of large-scale field accompanied by the generation of total magnetic flux.
- "Small-scale dynamo" sustainment of magnetic energy due to magnetic fluctuations in a turbulent state with a small amount of flux.

Signatures of dynamo: production of magnetic energy, flux and helicity out of no, or seed, field



• Can large-scale magnetic fields be generated through complex flows of plasmas (MHD dynamo)?



#### How could a large-scale field grow?

Consider: mean seed field + differential rotation

 $B_0$  and  $V_{\phi}(z)$ 



The Omega-effect:

Conversion of poloidal field to toroidal field by differential rotation (shear) of toroidal flows – (shear of the mean field by differential rotation)



#### Could a large-scale field grow out of turbulence?

Bn

Consider:

- $V = \langle V \rangle + \widetilde{V}$  $B = \langle B \rangle + \widetilde{B}$  $\uparrow \qquad \uparrow$ large-scale small-scale
  - fluctuations :  $\widetilde{\mathbf{B}}_{mn}(\mathbf{r}) = \widetilde{\mathbf{B}}_{mn}(\mathbf{r})e^{i(m\phi-nz+\delta)} + c.c$

+ + +

Β,

 <>, or overbars → azimuthally and axially averaged surface-averaged ∫ dφdz

$$\bullet < \widetilde{B} > = < \widetilde{V} > = 0$$

#### Unstratified Keplerian cylinder





### Magnetic field interacts with the velocity field of the fluid through the induction equation





#### Possible candidates for large-scale field generation

The  $\Omega$  and  $\alpha$  effects.



from Berger 99

Differential rotation provides a strong source of helicity injection and field growth  $\frac{\partial \overline{\mathbf{B}}}{\partial t} \propto \overline{\mathbf{B}}_0 \frac{d}{dz} \overline{\mathbf{V}}(z).$ 



$$\overline{\mathcal{E}}_{\textit{emf}} pprox < \widetilde{\textit{V}} imes \widetilde{\textit{B}} >$$

The electromotive force (EMF) from correlated velocity

and magnetic field fluctuations

$$\frac{\partial \overline{\mathbf{B}}}{\partial t} = \nabla \times \left( \overline{\mathbf{V}} \times \frac{\overline{\mathbf{B}}}{\overline{\mathbf{B}}} + \overline{\mathcal{E}}_{emf} - \eta \nabla \times \overline{\mathbf{B}} \right)$$

Beyond stellar and galactic contexts, evidence for large-scale field growth is seen in

- magnetically dominated laboratory plasmas [Ji et al. 1995; Cothran et al. 2009]
- local and global simulations [Brandenburg et al. 1995; Ebrahimi et al. 2009; Lesur & Ogilvie 2010; Gressel 2010; Davis et al. 2010; Simon et al. 2011; Guan & Gammie 2011; Sorathia et al. 2012; Rincon et al 2007; Vishniac 2009; Ebrahimi & Bhattacharjee 2014, Squire & Bhattacharjee 2015; Suzuki & Inutsuka 2014; Ebrahimi & Blackman 2016; Bhat et al. 2016,] of the magnetorotational instability (MRI) [Velikhov 1959; Balbus & Hawley 1991]



Flow-driven Magnetorotational Instability (MRI) turbulence in disk is an example of dynamo field generation



#### Evidence for large-scale field growth in local simulations of MRI



The yz averaged field here matches with that generated in global simulation of Ebrahimi and Blackman (2016). **Bhat, Ebrahimi & Blackman, MNRAS, 2016** 

Large-scale toroidal field generated in unstratified simulations. (averaged over vertical and toroidal directions in zero net-flux simulations)



Fatima Ebrahimi Magnetic fields - dynamo and reconnection 15

#### In 2-D, there is no generation of toroidal field or mean helicity

#### 2-D simulations



Initial uniform seed B fields toroidally stretched, but due to symmetry,  $\langle B_{\phi} \rangle = 0$ .  $\overline{\mathcal{E}} \cdot B = 0$  $B_z$  is amplified due to  $\overline{\mathcal{E}}_{\phi}$ . F. Ebrahimi et al. ApJ. 2009 Top view



### Mean toroidal field is generated in the presence of helical perturbation (3-D simulations)

- Field line visualizations during non-linear MRI simulations in a 3D cylinder when m = 1 mode perturbation is dominant.
- Toroidal top view in 3D shows the twisting of the field lines.



## Energy in both large-scale and small-scale is generated (3-D simulations)



Vertically and toroidally averaged components in our model.

$$\begin{split} & \Downarrow = \langle \widetilde{\mathbf{V}} \times \widetilde{\mathbf{B}} \rangle_{z} \\ & \frac{\partial \overline{\mathbf{B}}_{\phi}}{\partial t} = -\frac{\partial \overline{\mathcal{E}}_{z}}{\partial r} + \underbrace{(\overline{\mathbf{B}} \cdot \nabla) \overline{\mathbf{V}}|_{\phi}}_{\mathsf{Traditional}} - (\overline{\mathbf{V}} \cdot \nabla) \overline{\mathbf{B}}|_{\phi}, \\ & \uparrow \\ & \mathsf{Traditional} \ \Omega \text{ effect} = \overline{B}_{r} V_{\phi}' \\ & \frac{\partial \overline{\mathbf{B}}_{r}}{\partial t} = -\frac{\partial \overline{\mathcal{E}}_{\phi}}{\partial z} + \frac{\partial \overline{\mathcal{E}}_{z}}{\partial \phi} + (\overline{\mathbf{B}} \cdot \nabla) \overline{\mathbf{V}}|_{r} - (\overline{\mathbf{V}} \cdot \nabla) \overline{\mathbf{B}}|_{r} \\ & \frac{\partial \overline{\mathbf{B}}_{z}}{\partial t} = \frac{\partial \overline{\mathcal{E}}_{\phi}}{\partial r} + (\overline{\mathbf{B}} \cdot \nabla) \overline{\mathbf{V}}|_{z} - (\overline{\mathbf{V}} \cdot \nabla) \overline{\mathbf{B}}|_{z} \end{split}$$

**OPPPL PRINCETON** UNIVERSITY Mean  $B_{\phi}$  is generated through the vertical EMF, not the traditional  $\Omega$  effect.

$$\Downarrow = \langle \widetilde{\mathbf{V}} \times \widetilde{\mathbf{B}} \rangle_z$$

dr



## DNS shows that mean toroidal field is correlated with, and directly generated by the vertical EMF.



- What is the form of fluctuation-induced emf force?
- Can fluctuations inject magnetic helicity and generate flux?
- Do local magnetic helicity fluxes sustain large scale dynamo?

[F. Ebrahimi and A. Bhattacharjee PRL 2014]



### The alpha effect can be rigorously written in the form of a total divergence of the helicity flux from fluctuations

Local magnetic helicity variation is

$$\frac{\partial (\mathbf{A} \cdot \mathbf{B})}{\partial t} + \nabla \cdot \Gamma_k = -2\mathbf{E} \cdot \mathbf{B}.$$

Total helicity flux :  $\Gamma_k = -2\mathbf{A} \times \mathbf{E} - \mathbf{A} \times \frac{\partial \mathbf{A}}{\partial t}$ 

 It can be shown that fluctuation induced dynamo effect is expressed in a divergence form and dissipative terms.

$$\varepsilon_{emf} \cdot \overline{\mathbf{B}} = -\eta < \widetilde{\mathbf{J}} \cdot \widetilde{\mathbf{B}} > -\frac{1}{2} \frac{\partial}{\partial t} < \widetilde{\mathbf{A}} \cdot \widetilde{\mathbf{B}} > +H\alpha$$

Where;

$$H\alpha = -\frac{1}{2}\nabla \cdot < \Gamma_k >= \nabla \cdot [<\widetilde{\mathbf{A}} \times \widetilde{\mathbf{E}} > +\frac{1}{2} < \widetilde{\mathbf{A}} \times \frac{\partial}{\partial t} \widetilde{\mathbf{A}} >]$$

Nonlinear simulations show that the alpha effect can be written in terms of a total divergence for an MRI mode.



• Nonlinear m=1 MRI mode simulations show  $\langle \widetilde{\mathbf{V}} \times \widetilde{\mathbf{B}} \rangle \cdot \overline{\mathbf{B}} \approx -\nabla \cdot \langle \Gamma_k \rangle /2.$ 

















### Nature tries to get rid of magnetic helicity through magnetic reconnection

Would magnetic field be annihilated while being generated?

Magnetic reconnection:

- energizes many processes in nature
- is a major interplay for fundamental physical phenomena such as particle acceleration and heating, magnetic-field generation, and momentum transport



Magnetic reconnection is the rearrangement of magnetic field topology of plasmas – forced (driven) reconnection



This process occurs in the solar atmosphere, the solar wind, the Earth's magnetosphere, astrophysical disks, turbulence, and laboratory plasmas.



# Magnetic reconnection is the rearrangement of magnetic field topology of plasmas.





#### Current-driven magnetic reconnection - Tearing instability Spontaneous reconnection



#### Furth, Killeen, and Rosenbluth (1963)

#### THE PHYSICS OF FLUIDS

VOLUME 6, NUMBER 4

April 1963

#### Finite-Resistivity Instabilities of a Sheet Pinch

HAROLD P. FURTH AND JOHN KILLEEN Lawrence Radiation Laboratory, Livermore, California

IND

MARSHALL N. ROSENBLUTH

University of California, San Diego, La Jolla, California, and John Jay Hopkina Laboratory for Pure and Applied Science, General Atomic Division of General Dynamics Corporation, San Diego, California (Received 17 September 1962)

The stability of a plane current layer is analyzed in the hydromagnetic approximation, allowing for finite isotropic resistivity. The effect of a small layer curvature is simulated by a gravitational field. In an incompressible fluid, there can be three basic types of "resistive" instability; a long-wave "tearing" mode, corresponding to breakup of the layer along current-flow lines; a short-wave "rippling" mode, due to the flow of current across the resistivity gradients of the laver; and a low-q gravitational interchange mode that grows in spite of finite magnetic shear. The time scale is set by the resistive diffusion time  $\tau_{P}$  and the hydromagnetic transit time  $\tau_{P}$  of the layer. For large S - $\tau_{\rm R}/\tau_{\rm B}$ , the growth rate of the "tearing" and "ripping" modes is of order  $\tau_{\rm R}^{-5/5}\tau_{\rm R}^{-2/5}$ , and that of the gravitational mode is of order  $\tau_{\rm R}^{-1/3}\tau_{\rm R}^{-2/3}$ . As  $S \to \infty$ , the gravitational effect dominates and may be used to stabilize the two nongravitational modes. If the zero-order configuration is in equilibrium, there are no overstable modes in the incompressible case. Allowance for plasma compressibility somewhat modifies the "rippling" and gravitational modes, and may permit overstable modes to appear. The existence of overstable modes depends also on increasingly large zero-order resistivity gradients as  $S \rightarrow \infty$ . The three unstable modes merely require increasingly large gradients of the first-order fluid velocity; but even so, the hydromagnetic approximation breaks down as  $S \to \infty$ . Allowance for isotropic viscosity increases the effective mass density of the fluid, and the growth rates of the "tearing" and "rippling" modes then scale as  $\tau_R^{-2/3}\tau_R^{-1/3}$ . In plasmas, allowance for thermal conductivity suppresses the "rippling" mode at moderately high values of S. The "tearing" mode can be stabilized by conducting walls. The transition from the low-q "resistive" gravitational mode to the familiar high-g infinite conductivity mode is examined. The extension of the stability analysis to cylindrical geometry is discussed. The relevance of the theory to the results of various plasma experiments is pointed out. A nonhydromagnetic treatment will be needed to achieve rigorous correspondence to the experimental conditions.

#### I. INTRODUCTION

A PRINCIPAL result of pinch<sup>1,2</sup> and stellarator<sup>3</sup> research has been the observed instability of configurations that the hydromagnetic theory<sup>4,6</sup> would predict to be stable in the limit of high

<sup>1</sup> S. A. Colgate and H. P. Furth, Phys. Fluids 3, 982 (1960).
<sup>2</sup> K. Aitken, R. Bickerton, R. Hardcastle, J. Jukes, P.

electrical conductivity. In order to establish the cause of this observed instability, the extension of the hydromagnetic analysis to the case of finite conductivity becomes of considerable interest.

A number of particular "resistive" instability modes have been discussed in previous publications. Dungey<sup>8</sup> has shown that, at an x-type neutral point



Fatima Ebrahimi

### Spontaneous magnetic reconnection as the result of tearing fluctuations



with small perturbation



#### Magnetic reconnection

if  $\eta = \mathbf{0}$ 



$$\frac{d\mathbf{B}}{dt} = \nabla \times (\mathbf{V} \times \mathbf{B})$$

$$\widetilde{V}_r = \gamma \widetilde{B}_r / (k \cdot B) = = \gg \widetilde{B}_r = 0$$

**OPPPL PRINCETON** UNIVERSITY

### Magnetic reconnection occurs at finite resistivity



magnetic diffusion equation:

$$rac{d {f B}}{dt} = 
abla imes ({f V} imes {f B}) - rac{\eta}{\mu_0} 
abla^2 {f B}$$

• 
$$\widetilde{B}_r(\mathbf{r},t) \sim \widetilde{B}_r(\mathbf{r})\exp(ik_z z - i\omega t)$$

### Magnetic Reynolds number a measure of how closely the magnetic field is coupled to the fluid

**Dimensionless equation** 

$$rac{d \mathbf{B}}{dt} = \mathbf{S} 
abla imes (\mathbf{V} imes \mathbf{B}) - \eta 
abla^2 \mathbf{B}$$

measure of plasma resistivity, Lundquist number  $S = \tau_R/\tau_A$ 

$$au_{R} = \mu_{0} a^{2} / \eta$$
  $au_{A} = a / (B^{2} / (\mu_{0} \rho)^{1/2})$ 

Growth rate is a hybrid between resistive and Alfven times:

$$au_{growth} \sim au_{R}^{-3/5} au_{A}^{-2/5}$$
 ,  $\gamma au_{A} \propto S^{-3/5}$ 

In general magnetic Reynolds number  $Rm \equiv LV/\eta$ 



# Many fundamentals of reconnection physics can be explored during helicity injection



$$\frac{\partial K}{\partial t} = -2 \int (\mathbf{A} \cdot \mathbf{V}) \mathbf{B} \cdot d\mathbf{s}$$

Kusano 2004

Warnecke & Brandenburg 2010

#### Helicity injection in a lab



$$\frac{\partial K}{\partial t} = -2 \int \Phi \mathbf{B} \cdot d\mathbf{s}$$

Helicity is injected through a surface term.



Transient Coaxial Helicity Injection (CHI), the primary candidate for solenoid- free current start-up in spherical tokamaks





# Helicity injection simulations are performed using the extended-MHD NIMROD code

• Solves the linear and nonlinear MHD equations

$$\begin{aligned} \frac{\partial \mathbf{B}}{\partial t} &= -\nabla \times \mathbf{E} + \kappa_{divb} \nabla \nabla .\mathbf{B} \\ \mathbf{E} &= -\mathbf{V} \times \mathbf{B} + \eta \mathbf{J} + \frac{1}{ne} \mathbf{J} \times \mathbf{B} \\ \mathbf{J} &= \nabla \times \mathbf{B} \\ \frac{\partial n}{\partial t} + \nabla .(n\mathbf{V}) &= \nabla .D\nabla n \\ \rho(\frac{\partial \mathbf{V}}{\partial t} + \mathbf{V} . \nabla \mathbf{V}) &= \mathbf{J} \times \mathbf{B} - \nabla P - \nabla .\Pi \\ \frac{n}{(\Gamma - 1)} (\frac{\partial T_{\alpha}}{\partial t} + \mathbf{V} . \nabla T_{\alpha}) &= -p_{\alpha} \nabla .\mathbf{V} - \nabla .\mathbf{q}_{\alpha} + Q \end{aligned}$$

• 
$$\mathbf{q} = -n[(\kappa_{||} - \kappa_{\perp})\hat{b}\hat{b} + \kappa_{\perp}\mathbf{I}] \cdot \nabla T$$

- $\Pi$  is the stress tensor (also includes numerical  $\rho\nu\nabla V$ )
- κ<sub>divb</sub> and D are magnetic-divergence and density diffusivities for numerical purposes

During injection (V<sub>inj</sub> on)

During decay ( $V_{inj} = 0$ )





# Two types of current sheets are formed during flux expansion/evolution



 1- Edge current sheet from the poloidal flux compression near the plasma edge, leads to 3-D filament structures

 2- Primary reconnecting current sheet from the oppositely directed field lines in the injector region.

#### F. Ebrahimi PoP Letters 2016



#### Forced reconnection in the injection region



A local 2-D Sweet-Parker type reconnection is triggered in the injection region. Key signatures:

- I Elongated current sheets,
   L > δ.
- II Scaling of the current sheet width  $\delta/L \sim (1 + P_m)^{1/4} S^{-1/2}$  $\sim V_{in}/V_{out}$
- III -Pinch inflow and Alfvénic outflow

S =  $LV_A/\eta$  (Alfven velocity based on the reconnecting B, L is the current sheet length) F. Ebrahimi, et al. PoP 2013, 2014



# In many fast MHD dynamical processes, plasmoids are essential features

- Elongated current sheet can become tearing unstable at high S. [Biskamp 1986, Shibata & Tanuma 2001]
- The scaling properties of a classical linear tearing changes,  $(\gamma \sim S^{1/4})$ .

Numerical development: [Tajima &

Shibata 1997,Loureiro et al. 2007; Lapenta 2008; Daughton et al. 2009,; Bhattacharjee et al. 2009] **Show fast reconnection**. Static linear theory doesn't apply [L. Comisso et al. PoP 2016]



#### Spontaneous plasmoid reconnection





At high S, a transition to a plasmoid instability is demonstrated in the simulations.

Both small sized transient plasmoids and large system-size plasmoids are formed and co-exist. (S=39000)

Plasmoids merge to form closed flux surfaces. Reconnection rate becomes nearly independent of S.

F. Ebrahimi and R.Raman PRL 2015



Plasmoid instability with continued injection of plasmoids is observed during the injection phase (S  $\sim$  29000)



(Loading poloidalflux.mp4)

#### Dynamo-driven plasmoids formation

#### ► 3D effects

- Could large-scale dynamo from 3-D fluctuations trigger reconnecting plasmoids?
- Self-consistent trigger mechanism in 3-D?



## Edge current-sheet instabilities are triggered in 3-D, and break the current-sheet



- I- Edge-localized modes arising from the asymmetric current-sheet instabilities
- II- First observation of nonaxisymmetric edge current

 III- With 3-D fluctuations, axisymmetric plasmoids are formed, local S increased to S ~ 15000. [Ebrahimi PoP Letters 2016] Edge modes grow on the poloidal Alfven time scales

These modes grow fast, on the poloidal Alfven time scales, and are peeling modes with tearing-parity structures.

These modes saturate by modifying and relaxing the edge current sheet

$$\gamma au_{A(n=1)} = 0.16,$$
  
 $\gamma au_{A(n=2)} = 0.18,$   
 $\gamma au_{A(n=3)} = 0.2,$   
 $\gamma au_{A(n=4)} = 0.23,$   
 $\gamma au_{A(n=5)} = 0.26.$   
 $S = 2 \times 10^5$ 





### Poloidal flux amplification is observed to trigger axisymmetric reconnecting plasmoids formation



- For the first time a dynamo poloidal flux amplification is observed
- This fluctuation-induced flux amplification increases the local S

==>

### triggers a plasmoid instability

==> breaks the primary current sheet.



#### Observational evidence of plasmoid-like structures



Plasmoids

Camera images from NSTX do show the formation, and subsequent separation, of smaller plasmoids that then merge into a larger pre-existing plasma.[Ebrahimi&Raman PRL 2015]



Plasmoids (2D) of the reconnected plasma flowing along the current

sheet.LASCO/SOHO C3 images [Lin et al. 2005;

Reily et al. 2007]

